

What you will learn about:
Graphing Rational Functions

X-intercept

Let $y=0$ solve for x

Y-intercept

Let $x=0$ solve for y

$0 = x^2 - 36$
 $x^2 = 36$
 $x = \pm 6$
Find the X-intercept(s) and y-intercept of each function.

A) $f(x) = x^2 - 36$

X-intercept

$0 = x^2 - 36$

$0 = (x-6)(x+6)$

$x-6=0$ $x+6=0$

$x=6$ $x=-6$

Y-intercept

$y = 0^2 - 36$

$(0, -36)$

B) $f(x) = \frac{x-5}{x+3}$

X-intercept

$x-5=0$

$x=5$

Y-intercept

$y = \frac{0-5}{0+3} = -\frac{5}{3}$

C) $f(x) = \frac{x}{x+6}$

X-intercept

$x=0$

Y-intercept

$y = \frac{0}{0+6} = \frac{0}{6} = 0$

D) $\frac{x^2+4}{x+2}$

X-intercept

$x^2+4=0$

None

$x^2+4=0$

$x = \pm 2i$

Y-intercept

$y = \frac{0^2+4}{0+2} = \frac{4}{2} = 2$

E) $f(x) = \frac{x^2-3x-10}{x}$

$x^2-3x-10=0$

$(x-5)(x+2)=0$

$x-5=0$ $x+2=0$

$x=5$ $x=-2$

$\frac{0^2-3(0)-10}{0} = \frac{-10}{0}$

None

Domain
X-values (Inputs)

• Undefined values
make Bottom of
Fraction Zero

• Undefined values
can not be in Domain

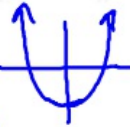
$$x^2 + 2x - 3 = 0$$

$$(x-1)(x+3) = 0$$

$$x=1 \quad x=-3$$

Find the domain of the function algebraically. Support your answer graphically

A) $f(x) = x^2 - 9$



$$D: (-\infty, \infty)$$

B) $f(x) = \frac{1}{x+5}$

$$x+5=0$$
$$x=-5$$

$$D: (-\infty, -5) \cup (-5, \infty)$$

C) $f(x) = \frac{x}{x^2 + 2x - 3}$

$$D: (-\infty, -3) \cup (-3, 1) \cup (1, \infty)$$

D) $f(x) = \frac{3}{x} + \frac{7}{x-1}$

$$x=0$$
$$x=1$$

$$D: (-\infty, 0) \cup (0, 1) \cup (1, \infty)$$

E) $f(x) = \frac{x+6}{x^2-36} = \frac{x+6}{(x-6)(x+6)}$

$$x=6, x=-6$$

$$D: (-\infty, -6) \cup (-6, 6) \cup (6, \infty)$$

Range y-values
(output)

Look at graph

Point of Discontinuity
Undefined value

• Vertical Asymptote
Value that makes
only bottom
zero

• Hole
Value makes top
and bottom
zero.

Determine the range of the function

A) $f(x) = 4 + x^2$

R: $[4, \infty)$

B) $f(x) = 2 + \sqrt{9-x}$

R: $[2, \infty)$

C) $f(x) = \frac{x^2}{4-x^2}$

R: $(-\infty, -1) \cup [0, \infty)$

D) $f(x) = \frac{3-2x^2}{4+x^2}$ $\frac{3-0}{4+0} = \frac{3}{4}$

R: $(-2, \frac{3}{4}]$

Graph the function and tell whether or not the function has a point of discontinuity at $x=0$. If there is a discontinuity, tell whether the discontinuity is removable (Hole) or non-removable (Vertical Asymptote).

A) $f(x) = \frac{5}{x}$

$f(0) = \frac{5}{0}$

Yes $x=0$ Point
of Discontinuity
Vertical Asymptote

B) $f(x) = \frac{x^2+x}{x}$

$f(0) = \frac{0^2+0}{0}$

$x=0$ is a Point of
Discontinuity

Hole

C) $f(x) = \frac{|5x|}{x}$

Yes $x=0$ P.O.D
Hole

D) $f(x) = \frac{2x}{x-4}$

$x=0$ Not P.O.D

Reminder:
Sometimes a value of x that seems to be a vertical asymptote is actually a hole

Horizontal Asymptote

- Degree on top is greater than degree on bottom

No H.A.

- If Degree on Bottom is greater than Degree on top H.A. $y=0$

- If Degrees are equal then HA is Ratio of Leading Coefficients

$$y = \frac{LC}{LC}$$

Find all horizontal and vertical asymptotes

A) $f(x) = \frac{x+1}{x}$

V.A. $x=0$

H.A. $y = \frac{1}{1} = 1$

~~B) $f(x) = 2^x$~~

C) $f(x) = \frac{-3x^2+1}{x^2-1}$

$$x^2-1=0$$

$$(x-1)(x+1)=0$$

$$x=1 \quad x=-1$$

V.A. $x=1, x=-1$

H.A. $y = \frac{-3}{1} = -3$

E) $f(x) = \frac{3x^3+3}{x^2+1}$

D) $f(x) = \frac{3x-9}{x^2-9}$

P.O.D = ~~$x=3$~~ , -3

V.A. $x=-3$

H.A. $y=0$

F) $f(x) = \frac{x+5}{x^3-27}$